

Comparison of Complexity of Chaos in Many Degrees of Freedom Chaotic Circuits

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Abstract—This paper considers comparison of the complexity of chaos generated in many degrees of freedom chaotic circuits. We increase the number of connected subcircuits from two to three in order to produce more complex chaos. By means of the circuit experiment and computer simulation, we show chaotic attractors. From the results, we confirmed that more complex chaos is generated in the each circuit.

I. INTRODUCTION

Chaos has two major features. They are initial value sensitivity and long-term unpredictability. It is difficult to predict long-term weather forecasts [1] due to initial values such as temperature, atmospheric pressure, and wind speed, etc.

Chaotic circuit is used to considers nonlinear phenomena such as natural phenomena. It is faster and easier to experiment than actual natural phenomena. Strictness analysis is difficult for chaotic phenomena generated in high-dimensional systems [2]. Therefore, getting closer to high-dimensional chaos that exists in nature leads to an effect that is useful for the real world from a new perspective. For example, it may be possible to improve the confidentiality of chaotic communications [3] or to be closer to human judgment in brain-type computers [4].

In this study, we investigate comparison of the complexity of chaos generated in many degrees of freedom chaotic circuits. In the previous study, the circuit consists of two Inaba's circuits coupled by one linear negative resister has proposed [5]. At this time, the circuit is set a different parameter values, especially natural frequencies for each circuit. Then we compare the two circuits in series with the three. We show chaotic attractors generated in the circuit experiment and computer simulation.

II. SYSTEM MODEL

In the previous study, we use the circuit model of two degrees of freedom chaotic circuit in Fig. 1. This circuit was expanded from the Inaba's circuit to two degrees of freedom chaotic circuit. In this circuit, the case where the natural frequency of the lower subcircuit was higher than the natural frequency of the upper subcircuit was investigated.

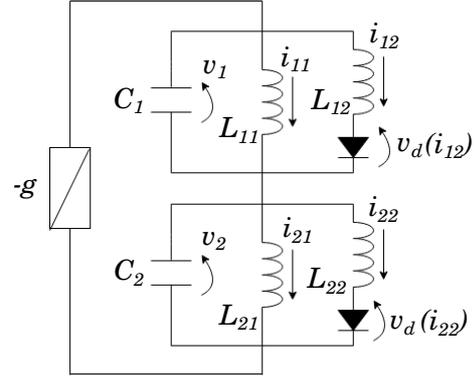


Fig.1 Circuit model of two degrees of freedom chaotic circuit.

The parameters are described as follows:

$$t = \sqrt{L_{11}C_1}\tau, \text{ " . " } = \frac{d}{d\tau}, \alpha = g\sqrt{\frac{L_{11}}{C_1}},$$

$$\beta_1 = \frac{L_{11}}{L_{12}}, \beta_2 = \frac{L_{11}}{L_{21}}, \beta_3 = \frac{L_{11}}{L_{22}},$$

$$\gamma = \frac{C_1}{C_2}, \varepsilon = \frac{1}{r_d}\sqrt{\frac{L_{11}}{C_1}},$$

$$v_1 = Ex_1, i_{11} = E\sqrt{\frac{C_1}{L_{11}}}x_2, i_{12} = E\sqrt{\frac{C_1}{L_{11}}}x_3,$$

$$v_2 = Ex_4, i_{21} = E\sqrt{\frac{C_1}{L_{11}}}x_5, i_{22} = E\sqrt{\frac{C_1}{L_{11}}}x_6.$$

The normalized circuit equations are described as follows:

$$\begin{cases} \dot{x}_1 = \alpha(x_1 + x_4) - (x_2 + x_3) \\ \dot{x}_2 = x_1 \\ \dot{x}_3 = \beta_1(x_1 - f(x_3)) \\ \dot{x}_4 = \alpha\gamma(x_1 + x_4) - \gamma(x_5 + x_6) \\ \dot{x}_5 = \beta_2x_4 \\ \dot{x}_6 = \beta_3(x_4 - f(x_6)). \end{cases} \quad (1)$$

The characteristic equation for the diode is described as follows:

$$f(x) = \frac{1}{2\varepsilon}(x + \varepsilon - |x - \varepsilon|). \quad (2)$$

III. PROPOSED SYSTEM

In this study, we use the circuit model of three degrees of freedom chaotic circuit in Fig. 2. This circuit consists of two degrees of freedom chaotic circuit and another Inaba's circuit connected in series in order to produce more complex chaos.

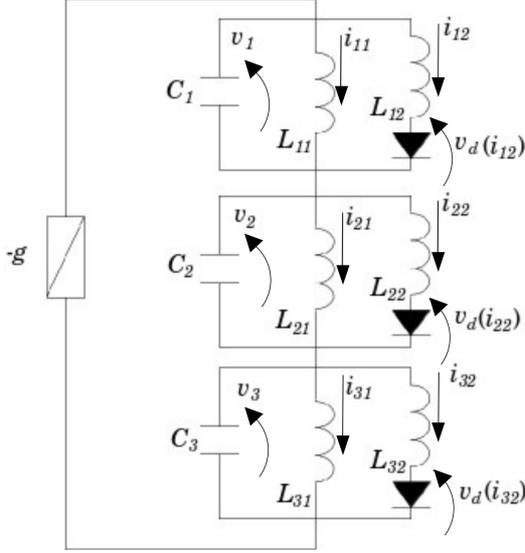


Fig.2 Circuit model of three degrees of freedom chaotic circuit.

The parameters are described as follows:

$$t = \sqrt{L_{11}C_1}\tau, \quad \tau = \frac{d}{d\tau}, \quad \alpha = g\sqrt{\frac{L_{11}}{C_1}},$$

$$\beta_1 = \frac{L_{11}}{L_{12}}, \quad \beta_2 = \frac{L_{11}}{L_{21}}, \quad \beta_3 = \frac{L_{11}}{L_{22}}, \quad \beta_4 = \frac{L_{11}}{L_{31}}, \quad \beta_5 = \frac{L_{11}}{L_{32}},$$

$$\gamma_1 = \frac{C_1}{C_2}, \quad \gamma_2 = \frac{C_1}{C_3}, \quad \varepsilon = \frac{1}{rd}\sqrt{\frac{L_{11}}{C_1}},$$

$$v_1 = Ex_1, \quad i_{11} = E\sqrt{\frac{C_1}{L_{11}}}x_2, \quad i_{12} = E\sqrt{\frac{C_1}{L_{11}}}x_3,$$

$$v_2 = Ex_4, \quad i_{21} = E\sqrt{\frac{C_1}{L_{11}}}x_5, \quad i_{22} = E\sqrt{\frac{C_1}{L_{11}}}x_6,$$

$$v_3 = Ex_7, \quad i_{31} = E\sqrt{\frac{C_1}{L_{11}}}x_8, \quad i_{32} = E\sqrt{\frac{C_1}{L_{11}}}x_9.$$

The parameters are described as follows:

$$\begin{cases} \dot{x}_1 = \alpha(x_1 + x_4 + x_7) - (x_2 + x_3) \\ \dot{x}_2 = x_1 \\ \dot{x}_3 = \beta_1(x_1 - f(x_3)) \\ \dot{x}_4 = \alpha\gamma_1(x_1 + x_4 + x_7) - \gamma_1(x_5 + x_6) \\ \dot{x}_5 = \beta_2x_4 \\ \dot{x}_6 = \beta_3(x_4 - f(x_6)) \\ \dot{x}_7 = \alpha\gamma_2(x_1 + x_4 + x_7) - \gamma_2(x_8 + x_9) \\ \dot{x}_8 = \beta_4x_7 \\ \dot{x}_9 = \beta_5(x_8 - f(x_9)). \end{cases} \quad (3)$$

The characteristic equation for the diode is described as follows:

$$f(x) = \frac{1}{2\varepsilon}(x + \varepsilon - |x - \varepsilon|). \quad (4)$$

IV. RESULTS

A. Two degrees of freedom chaotic circuit

We show the experimental and computer simulation results of two degrees of freedom chaotic circuit in Fig. 1. Fig. 3 (a) is the result of the top circuit from circuit experiment. Fig. 3 (b) is the result of the top circuit from computer simulation. Fig. 4 (a) is the result of the bottom circuit from circuit experiment. Fig. 4 (b) is the result of the bottom circuit from computer simulation.

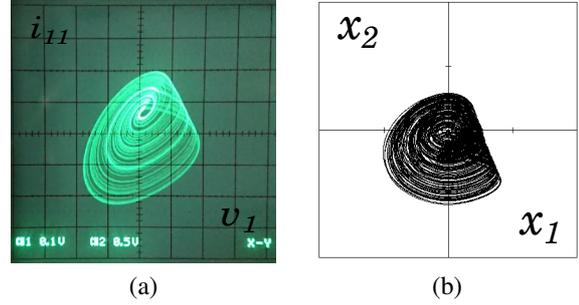


Fig. 3 Chaotic attractors in the top circuit.

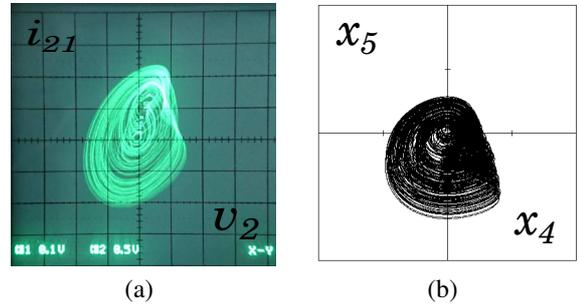


Fig. 4 Chaotic attractors in the bottom circuit.

In the circuit experiment, the circuit parameters are chosen as $C_1 = 15[nF]$, $L_{11} = 300[mH]$, $L_{12} = 30[mH]$, $C_2 = 7.5[nF]$, $L_{21} = 150[mH]$, and $L_{22} = 15[mH]$. In the computer simulation, the circuit parameters are chosen as $\alpha = 0.3$, $\beta_1 = 10.0$, $\beta_2 = 2.0$, $\beta_3 = 20.0$, $\gamma = 2.0$, and $\varepsilon = 0.01$.

As a result, the same attractors were observed qualitatively in each circuit in circuit experiment and computer simulation.

B. Three degrees of freedom chaotic circuit

In this study, we change the number of Inaba's circuit connected from two to three. We show the experimental and computer simulation results of three degrees of freedom chaotic circuit. Fig. 5 (a) is the result of the top circuit from circuit experiment. Fig. 5 (b) is the result of the top circuit from computer simulation. Fig. 6 (a) is the result of the middle circuit from circuit experiment. Fig. 6 (b) is the result of the middle circuit from computer simulation. Fig. 7 (a) is the result of the bottom circuit from circuit experiment. Fig. 7 (b) is the result of the bottom circuit from computer simulation.

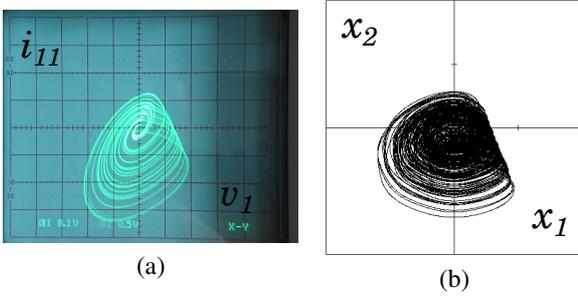


Fig. 5 Chaotic attractors in the top circuit.

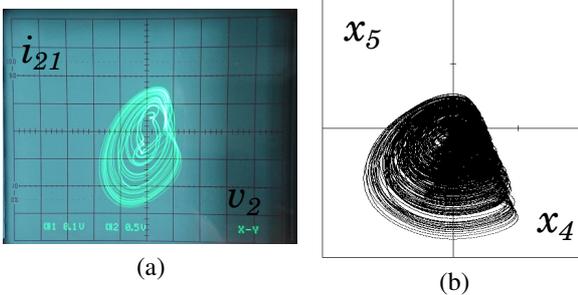


Fig. 6 Chaotic attractors in the middle circuit.

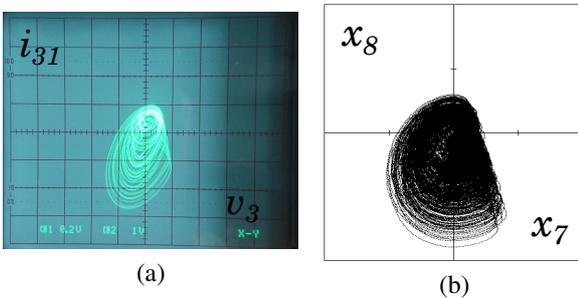


Fig. 7 Chaotic attractors in the bottom circuit.

In the circuit experiment, the circuit parameters are chosen as $C_1 = 15[nF]$, $L_{11} = 300[mH]$, $L_{12} = 30[mH]$, $C_2 = 7.5[nF]$, $L_{21} = 150[mH]$, $L_{22} = 15[mH]$, $C_3 = 5[nF]$, $L_{31} = 100[mH]$, and $L_{32} = 10[mH]$. In the computer simulation, the circuit parameters are chosen as $\alpha = 0.3$, $\beta_1 = 10.0$, $\beta_2 = 2.0$, $\beta_3 = 20.0$, $\beta_4 = 3.0$, $\beta_5 = 30.0$, $\gamma_1 = 2.0$, $\gamma_2 = 3.0$, and $\varepsilon = 0.01$.

Comparing the results of two degrees and three, attractors are similar in shape, and become more complex. The newly connected circuit generates more complex chaotic attractor.

V. CONCLUSION

In this study, we have investigated comparison of the complexity of chaos generated in multiple Inaba's circuit in series. We have increased the number of connected subcircuits from two to three in order to produce more complex chaos. We have evaluated the complexity using attractors obtained by circuit experiment and computer simulation. First, results of circuit experiment and computer simulation were qualitatively the same in the same circuit. Focusing on the chaotic attractor, more complex chaos is generated in the new connected circuit. When we compare the same circuits, it seems that attractors become more complex.

As our future work, we will clearly evaluate the difference in complexity by using Poincare map. In addition, we will research on various network types. We will investigate interactions between systems [6]. We regard three degrees of freedom chaotic circuits as one system, and they will be coupled using an inductor. First, we will investigate by connecting two chaotic circuits and increasing the number of connections. At this time, we will use a network topology such as ladders, rings, and stars to investigate basic networks [7].

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