Effectiveness of Combination of Artificial Immune System and Virus Theory of Evolution for QAPs

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Abstract—This paper presents the solving method of Quadratic Assignment Problems (QAPs). This method uses both Artificial Immune System (AIS) and Virus Theory of Evolution (VTE), and we call it Evolutionary Algorithm with Immune and Infection (EAII). EAII has characteristics of both AIS and VTE. We consider that EAII is effective method for QAPs. Thus, we apply EAII to the QAPs and confirm that EAII obtains more effective result than IA. Furthermore, we analyze the reason for obtaining better solution in EAII.

1. Introduction

Optimization problem is the problem to analyze state of maximum or minimum value in the function of a specific set. Some optimization problems are difficult to find the optimum solution. For example, these problems are Function Optimization Problem [1], Traveling Salesman problem [2], Knapsack Problem [3] and so on. Quadratic Assignment Problem (QAP) [4],[5] is known as one of difficult problems to find the optimum solution.

Artificial Immune System (AIS) [6] is computer system based on immune system of living organisms. AIS is able to apply to a variety of fields [7],[9]; optimization problems, pattern recognition, robotics and so on. Immune Algorithm (IA) [10]-[12] is based on AIS and is devised in immune system of possessing organisms. IA finds optimal solution by updating antibody group.

In this study, we focus attention on infection algorithm. The infection algorithm is based on Virus Theory of Evolution (VTE) [13]-[15]. Characteristic of VTE seems to be useful for finding the approximate solution quickly. If we propose the algorithm to use both infection algorithm and immune system, we can make a prediction that this algorithm obtains better result than IA. Thus, we propose Evolutionary Algorithm with Immune and Infection (EAII). EAII is the hybrid method of infection algorithm and IA. We carry out computer simulations for various parameter values and confirm that the proposed algorithm of EAII achieves better performance than other methods.

2. Quadratic Assignment Problem

The Quadratic Assignment Problem (QAP) [4],[5] is demanded looking for the best allocation of activities in locations. Task of the QAP is to assign all activities to different locations with the minimum cost among all combinations. The QAP has two matrices (F and D) of the dimension n×n (n indicates the size of problems). The matrix of F indicates each flow of activity, and the matrix of D indicates each distance. In using F and D, total assignment cost E(P) is shown as Eq. (1).

\[ E(P) = \sum_{i=1}^{n} \sum_{j=1}^{n} f_{ij} d_{P(i)P(j)} \]  

(1)

where \( f_{ij} \) and \( d_{P(i)P(j)} \) are (i,j)-th elements of D and F, \( P(i) \) (\( P(j) \)) is a alignment value.

For example, the matrix of F and D are defined by Eqs. (2) and (3). Figures 2 and 3 can indicate Eqs. (2) and (3). If f of flow allocate \( P(f2, f1, f4, f3) \) to \( (d1, d2, d3, d4) \) like Fig. 1, calculation result of \( E(P) \) is shown as Eq. (4).

\[ F = \begin{bmatrix} 0 & 5 & 10 & 2 \\ 5 & 0 & 6 & 3 \\ 10 & 6 & 0 & 4 \\ 2 & 3 & 4 & 0 \end{bmatrix} \]  

(2)

\[ D = \begin{bmatrix} 0 & 21 & 11 & 44 \\ 21 & 0 & 12 & 30 \\ 11 & 12 & 0 & 9 \\ 44 & 30 & 9 & 0 \end{bmatrix} \]  

(3)

\[ E(P) = \sum_{i=1}^{4} \sum_{j=1}^{4} f_{ij} d_{P(i)P(j)} \]  

(4)

If the size of n increases, the total combination of allocation explodes. The task of QAP is to demand minimum value of \( E(P) \).
3. Virus Theory of Evolution

Organic evolution is theory based on natural selection. In natural world, individuals of high fitness survive, while individuals of low fitness organism become extinct. Over the years, only higher fitness individuals survive. We call it Evolution. Thus, evolution needs to overlay generations.

On the other hand, Virus Theory of Evolution (VTE) [13] has proposed aside from organic evolution. This theory is based on the evolution by Lateral Gene Transfer (LGT) [14] in Virus infection. LGT is uptake of the gene to occur between other individuals and among other species. Without evolution inherited from parent cell to child cell, genes can evolve. Low fitness individuals possibly evolve into high fitness individuals in just one generation by LGT in Virus infection. Algorithms of using VTE was proposed in the past [15]. We assume using VTE algorithm leads the approximate solution in less time and VTE theory is efficient for the QAP.

4. Evolutionary Algorithm with Immune and Infection

Evolutionary Algorithm with Immune and Infection (EAlII) is based on AIS [10],[11] and VTE. Flow chart of EAlII is shown in Fig. 4. Flow of EAlII shows Steps1-5. Step2 from Step5 is repeated until the set iteration ($t_{max}$).

**Step1 Initialization**

We prepare a number of random location selection. We define the number of random locations as antibodies. The number of random locations selection is $U$.

**Step2 Evaluation of antibodies**

**Level of affinity**

Level of affinity indicates evaluation value, and is defined by the following Eq. (5).

$$\phi_v = \frac{1}{E(v)}$$

(5)

**Degree of similarity**

Degree of similarity of antibody $v$ and $w$ is defined by the following Eq. (6).

$$\Psi_{vw} = \frac{1}{1 + H_{vw}}$$

(6)

$H_{vw}$ indicates hamming distance of $v$ and $w$. Thus, when $v$ and $w$ are exactly the same, $H_{vw}$ equals 0.

**Concentration**

Concentration is defined by the following Eq. (7),(8). ($U$: Number of antibodies)

$$\Theta_v = \frac{1}{U} \sum_{w=1}^{U} \pi_{vw}$$

(7)

$$\pi_{vw} = \begin{cases} 1 & (\Psi_{vw} \geq T_1) \\ 0 & (\Psi_{vw} < T_1) \end{cases}$$

(8)

When $\Psi_{vw}$ cross threshold of $T_1$, $\pi_{vw}$ reflects $\Theta_v$.  

Figure 1: Example of QAP ($n = 4$).

Figure 2: Flow of activity.

Figure 3: Distance.

Figure 4: Flow chart of EAlII.
Step 3: Differentiation

Memory cell

This section is differentiation of antibodies into memory cell. If concentration \( \theta_i \) of each antibody \( v \) cross threshold of \( T_2 \), \( v \) changes candidate memory cell \( \mu \). When \( \mu \) do not reach a upper limit of number of memory cells, \( \mu \) becomes differentiated into memory cell. While \( \mu \) reach a upper limit of number of memory cells, we calculate degree of similarity \( \Psi_{pm} \) of \( \mu \) and \( m \). When evaluation value of \( \Psi_{pm} \) cross highest value of \( \Psi_{pm} \), \( \mu \) becomes differentiated into memory cell.

\( T \) cell

This sections differentiation of antibodies into \( T \) cell. \( v \) becomes differentiated into \( T \) cell \( t \) in descending order of concentration. We calculate degree of similarity \( \Psi_{vt} \) of \( v \) and \( t \). If \( \Psi_{vt} \) of \( T_2 \) \( v \) become extinct. This behavior indicates inhibition of similar solution. Extinct antibodies replenish new antibodies by random numbers.

Step 4: Promotion and Inhibition of production antibodies

Extinction and existence

We calculate level of affinity \( \phi_v \) by all antibodies \( v \). Number of \( \Psi_{vt} \) of \( v \) exist in descending order of \( \phi_v \). While, other \( \Psi_{vt} \) of \( v \) become extinct.

Production new antibodies

In surviving antibodies \( v \), new antibodies are produced by Crossover. Crossover is to be mated the two locations like Fig. 5.

Step 5: Infection

We select one memory cell. New antibodies are infected by a part of element of selected memory cell. Selected memory cell changes each time, and the selected number of element is decided with fixed probability. Part of antibody changes the information held like Fig. 6. We call it Infection. In this study, we define Infection rate. Infection rate indicates a fraction that antibodies group acquire the Infection.

5. Simulation Results

In order to compare the performance of EAlI and IA, we apply to find approximate solutions in QAPs. In this study, the number of \( t_{max} \) is 4000 times, the number of simulation is 10 times, \( U \) is 1024, applying QAP type are 5 kinds [5]. error rate is defined by the following Eq. (9).

\[
\text{Error rate}\% = \frac{(\text{obtain}) - (\text{optimum})}{(\text{optimum})} \times 100
\]  

where obtain denotes obtained solution and optimum shows optimum solution. When obtain value approaches optimum value, Error rate is low.

Tables 9 shows result of EAlI and IA. IA is same the number of \( t \) and \( U \) for comparing performance of EAlI. Infection rate in EAlI is 20%. We use these parameters of the each best result by simulation results. In results of Table 1, we confirm that EAlI obtains the better solution than IA.

<table>
<thead>
<tr>
<th>QAP type</th>
<th>Size</th>
<th>IA</th>
<th>EAlI</th>
</tr>
</thead>
<tbody>
<tr>
<td>tai12a</td>
<td>12</td>
<td>6.15</td>
<td>1.05</td>
</tr>
<tr>
<td>scr12</td>
<td>12</td>
<td>2.58</td>
<td>0.00</td>
</tr>
<tr>
<td>ngl20</td>
<td>20</td>
<td>9.51</td>
<td>6.85</td>
</tr>
<tr>
<td>had20</td>
<td>20</td>
<td>2.62</td>
<td>1.07</td>
</tr>
<tr>
<td>ngl30</td>
<td>30</td>
<td>14.23</td>
<td>12.42</td>
</tr>
</tbody>
</table>

Second, we focus on distribution of solutions. We investigate distribution of solutions by EAlI and IA in ngl30 (\( t_{max} = 4000, U = 1024 \)). Figure 7 shows sort solutions by high cost of E(P). Horizontal axis is the number of memory cell, and vertical axis is the cost of E(P). Initialization of EAlI and IA are same configuration, and number of memory cells are 50. Distributions of solutions are almost same in memory cells by EAlI and IA. However, the result of EAlI is better than IA. Thus, EAlI keeps diverse solution and obtains good result.
Figure 7: Distribution of solutions in nug20.

Third, we investigate calculation time and evaluation value by changing the number of memory cell. The number of memory cell is changed from 5 to 100, the number of simulation is 5 times, each value uses average value by 5 times, and QAP type is nug30 ($t_{max} = 4000, U = 1024$). Figure 8 shows relationship between the number of memory cell and calculation time, and Fig. 9 shows relationship between number of memory cell and evaluation value. If number of the memory cell increases, calculation time also increases. While, if the number of memory cell increases, EAI does not obtain good solution. Thus, we need to set the appropriate number of memory cell.

Figure 8: Relationship between number of the memory cell and calculation time (nug30).

Figure 9: Relationship between number of the memory cell and evaluation value (nug30).

6. Conclusions

We proposed EAI for solving the QAP, and compared the performance of EAI and IA to lead approximate solutions. From the result, the result of EAI was better result than IA. EAI obtained all kinds of evaluation value, and it is important to keep of diverse solution in solving solution of the QAP. Thus, it was efficient to use VTE based on IA in the QAP. We expect that apply these results to technological application possibility. In future work, we would like to study the mechanism of Infection in detail. We expect to obtain a better solution by studying mechanism of Infection.

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References