Abstract—In this study, we research a new layer arrangement of three layer cellular neural network (CNN). In this paper, we investigate the output characteristics by using our proposed method to image processing of gray scale image and binary image and show its effectiveness with simulation results.

I. INTRODUCTION

Cellular Neural Networks (CNN) were introduced by Chua and Yang in 1988 [1][2]. The idea of the CNN was inspired from the architecture of the cellular automata and the neural networks. The CNN has local connectivity property and they have been successfully developed in various image processing applications. Compare to the conventional neural networks, the CNN has been researched in various ways such as image processing and pattern recognition. In previous study of CNN, single-layer CNN have been introduced with many types of templates and after that, two-layer CNN have been proposed for high performance processing [3]. Recently, to obtain high performance in color image processing, three-layer CNN have been proposed [4].

In this study, we are using a new layer arrangement of three-layer CNN by using three types of templates. We investigate the output characteristics between the conventional CNN, two-layer CNN and the proposed CNN by apply to the binary image and gray-scale image to remove noise and edge detection simultaneously. In this paper, we describe about conventional CNN, two-layer CNN, three-layer CNN and proposed CNN in Sec. II. In Sec. III, we show simulation results of conventional CNN, two-layer CNN and proposed CNN respectively. In Sec. III also we compare between all types of structure CNN. Finally, we conclude our study in Sec. IV.

II. DEVELOPMENT OF THE STRUCTURE CNN

In this section, we explain about the development and the characteristics of the structure CNNs which are conventional CNN, two-layer CNN, three-layer CNN and our proposed structure.

A. Conventional CNN

Conventional CNN is the first CNN proposed in [1] and only had single layer. This means that the conventional CNN has only one type of process can be done in one process. For some image processing, two or more processes have to be done to obtain the result.

B. Two-layer CNN

To obtain better result in some image processing, two-layer CNN has been introduced [3]. Two-layer CNN is combination of two single-layer CNNs. The two single-layer CNNs are connected by using coupling templates $C_1$ and $C_2$ which are used to connect and transferred the data between first and second layers. Compare to the conventional CNN, two-layer CNN can be used two or more templates in one process. In our previous study [3], the two-layer CNN has been confirmed to have more efficient than single-layer CNN for some image processing.

C. Three-layer CNN

To overcome and obtain better results in color image processing, three-layer CNN have been proposed in our previous study [4]. There also have been several types of three-layer CNN. Like the two-layer CNN, to transfer between every single layers, three single CNNs are connected by using three coupling templates $C_1$, $C_2$ and $C_3$. In our previous study [4], three-layer CNN have been confirmed to have efficient results in color image processing.

D. Proposed CNN

In this study, we introduce a new structure of the CNN. The block diagram of the proposed CNN is shown in Fig. 1.

Figure 1 shows that the output of the first layer CNN (CNN1) is delivered into the second layer CNN (CNN2) and the third layer CNN (CNN3) by through coupling template $(C_1)$. In other way, the outputs of the CNN2 and the CNN3 are delivered into the CNN1 by through coupling templates $(C_2)$ and $(C_3)$, respectively. In the previous study of three-layer CNN [3], all three single-layer CNNs have mutual
connection between them. However, in our proposed CNN, CNN2 and CNN3 have not directly interacted between each layer. This arrangement is the different point between the previous structure of three-layer CNN and the proposed CNN.

The equations of the proposed CNN are described as below:

(1) State equations of the proposed CNN:

State equation of CNN1 :
\[
\frac{dv_{1i,j}}{dt} = -\frac{1}{R} v_{1i,j} + \sum_{k=i-r}^{i+r} \sum_{l=j-r}^{j+r} A_{1}(i, j; k, l) v_{qkl}(t) \\
+ \sum_{k=i-r}^{i+r} \sum_{l=j-r}^{j+r} B_{1}(i, j; k, l) v_{nkl}(t) \\
+ \sum_{k=i-r}^{i+r} \sum_{l=j-r}^{j+r} C_{1}(i, j; k, l) v_{q2kl}(t) \\
+ \sum_{k=i-r}^{i+r} \sum_{l=j-r}^{j+r} C_{3}(i, j; k, l) v_{q3kl}(t) + I_{1} \\
\text{if } |k-i| \leq 1 , |j-l| \leq 1.
\]

State equation of CNN2 :
\[
\frac{dv_{2i,j}}{dt} = -\frac{1}{R} v_{2i,j} + \sum_{k=i-r}^{i+r} \sum_{l=j-r}^{j+r} A_{2}(i, j; k, l) v_{q2kl}(t) \\
+ \sum_{k=i-r}^{i+r} \sum_{l=j-r}^{j+r} B_{2}(i, j; k, l) v_{n2kl}(t) \\
+ \sum_{k=i-r}^{i+r} \sum_{l=j-r}^{j+r} C_{1}(i, j; k, l) v_{q1kl}(t) + I_{2} \\
\text{if } |k-i| \leq 1 , |j-l| \leq 1.
\]

State equation of CNN3 :
\[
\frac{dv_{3i,j}}{dt} = -\frac{1}{R} v_{3i,j} + \sum_{k=i-r}^{i+r} \sum_{l=j-r}^{j+r} A_{3}(i, j; k, l) v_{q3kl}(t) \\
+ \sum_{k=i-r}^{i+r} \sum_{l=j-r}^{j+r} B_{3}(i, j; k, l) v_{n3kl}(t) \\
+ \sum_{k=i-r}^{i+r} \sum_{l=j-r}^{j+r} C_{1}(i, j; k, l) v_{q2kl}(t) + I_{3} \\
\text{if } |k-i| \leq 1 , |j-l| \leq 1.
\]

(2) Output equations of the proposed CNN:

Output equation of CNN1 :
\[
v_{y1i,j}(t) = \frac{1}{2}(v_{x1i,j}(t) + 1) - |v_{x1i,j}(t) - 1|.
\]

Output equation of CNN2 :
\[
v_{y2i,j}(t) = \frac{1}{2}(v_{x2i,j}(t) + 1) - |v_{x2i,j}(t) - 1|.
\]

Output equation of CNN3 :
\[
v_{y3i,j}(t) = \frac{1}{2}(v_{x3i,j}(t) + 1) - |v_{x3i,j}(t) - 1|.
\]
**Template of CNN1**:

\[
A_1 = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 1 \\ 1 & 1 & 1 \end{bmatrix}, \quad B_1 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \quad I_1 = 0. \tag{13}
\]

**Template of CNN2**:

\[
A_2 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \quad B_2 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \quad I_2 = -1. \tag{14}
\]

**Template of CNN3**:

\[
A_3 = \begin{bmatrix} 1 & 2 & 1 \\ 0 & 1 & 0 \end{bmatrix}, \quad B_3 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \quad I_3 = -0.5. \tag{15}
\]

**Coupling Templates**:

\[
C_1 = \begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}, \quad C_2 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix},
\]
\[
C_3 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & 0 \end{bmatrix}. \tag{16}
\]

**Remark:** In this study, we did not simulate the three-layer CNN [4] because we did not obtain good designed templates.

However, the conventional CNN needs two processes to obtain the desired result compared to the proposed CNN. First process, we apply “Small object remover” to remove the noises. Then, for the second process, we apply “Edge detection” to detect the edge of square. From these conclusions, we can say that the proposed CNN exhibited excellent performance than the conventional CNN and the two-layer CNN in these simulations.

**Remark:** We did not use template “Smoothing” in the conventional CNN and the two-layer CNN because less effective.

![Image](a)

**Template of CNN1**:

\[
A_1 = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 1 \\ 1 & 1 & 1 \end{bmatrix}, \quad B_1 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \quad I_1 = 0. \tag{13}
\]

**Template of CNN2**:

\[
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\]

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\[
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**Remark:** In this study, we did not simulate the three-layer CNN [4] because we did not obtain good designed templates.

Figure 2 shows the simulation results of binary images. Figure 2(a) shows an initial image which is a black square with noises. Figures 2(b), (c) and (d) show the outputs of the conventional CNN, the two-layer CNN and the proposed CNN for binary images, respectively. In Figs. 2(b), (c) and (d), the outputs show the edge of square can be detected. In noise removal’s performance, the outputs of the conventional CNN and proposed CNN show noises can be removed completely. However, the output of the two-layer CNN cannot remove noises completely. The results show that two-layer CNN cannot perform effectively in some image processing. From these simulation results, the conventional CNN and the proposed CNN show better results than the two-layer CNN.

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\]

**Template of CNN2**:

\[
A_2 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \quad B_2 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \quad I_2 = -1. \tag{14}
\]

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\[
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However, the conventional CNN needs two processes to obtain the desired result compared to the proposed CNN. First process, we apply “Small object remover” to remove the noises. Then, for the second process, we apply “Edge detection” to detect the edge of square. From these conclusions, we can say that the proposed CNN exhibited excellent performance than the conventional CNN and the two-layer CNN in these simulations.

**Remark:** We did not use template “Smoothing” in the conventional CNN and the two-layer CNN because less effective.

![Image](a)

Figure 3 shows the simulation results of gray-scale images. Figure 3(a) shows an initial image which is a black circle with noises. Figures 3(b), (c) and (d) show the outputs of the conventional CNN, the two-layer CNN and the proposed CNN for gray-scale images, respectively. In Figs. 3(b), (c) and (d), the outputs show that the edge of circle can be detected. In noise removal’s performance, although all of the outputs cannot remove noises completely, the outputs of the conventional CNN and the proposed CNN show slightly better than the two-layer CNN. These results also show that the two-layer CNN cannot perform effectively in some image processing. For the outputs of the conventional CNN and the proposed CNN, even the simulation results show almost the same, the output of the proposed CNN shows slightly better than the two-layer CNN. However, we can say that proposed CNN shows slightly better than conventional CNN and two-layer CNN.

![Image](a)

Figure 3 shows the simulation results of gray-scale images. Figure 3(a) shows an initial image which is a black circle with noises. Figures 3(b), (c) and (d) show the outputs of the conventional CNN, the two-layer CNN and the proposed CNN for gray-scale images, respectively. In Figs. 3(b), (c) and (d), the outputs show that the edge of circle can be detected. In noise removal’s performance, although all of the outputs cannot remove noises completely, the outputs of the conventional CNN and the proposed CNN show slightly better than the two-layer CNN. These results also show that the two-layer CNN cannot perform effectively in some image processing. For the outputs of the conventional CNN and the proposed CNN, even the simulation results show almost the same, the output of the proposed CNN shows slightly better than the two-layer CNN. However, we can say that proposed CNN shows slightly better than conventional CNN and two-layer CNN.
IV. CONCLUSION

In this study, we have proposed a new layer arrangement of three-layer CNN. In the proposed CNN, we use only one single layer CNN to connect with the other two single layer CNNs. From the computer simulations of simple images for binary image and gray-scale image, we investigated the output characteristics of the conventional CNN, two-layer CNN and proposed CNN. We can say that the proposed CNN have potential in image processing. However, at the moment, we do not say that our proposed CNN show excellent performance that conventional CNN and two-layer CNN.

In future works, we would like to use another type of images like an image which has scenery. We also would like to use another type of templates to apply in our proposed CNN.

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REFERENCES


